

## HAWC2 - Course

### Lesson 1: Defining the Structure

$$f(x+\Delta x) = \sum_{i=0}^{\infty} \frac{(\Delta x)^i}{i!} f^{(i)}(x) = \int_a^b \epsilon \Theta + \Omega \int \delta e^{i\pi} = \{2.7182818284\}$$

Risø DTU  
National Laboratory for Sustainable Energy

## What is a multibody formulation?

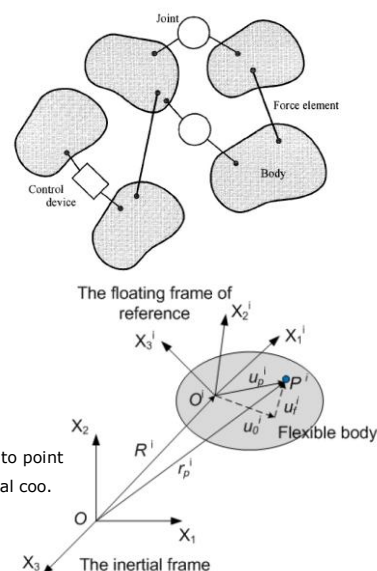
- A general coupling method for independent structural objects (rigid or flexible). Method used also referred to as floating frame of reference.
- Large rotations and translation are accounted for in the coupling point.
- Small deflections are assumed within the objects
- Couplings are done using algebraic constraints (fixed relative position, joints, controlled position etc.)

Position of a point on an object  $i$

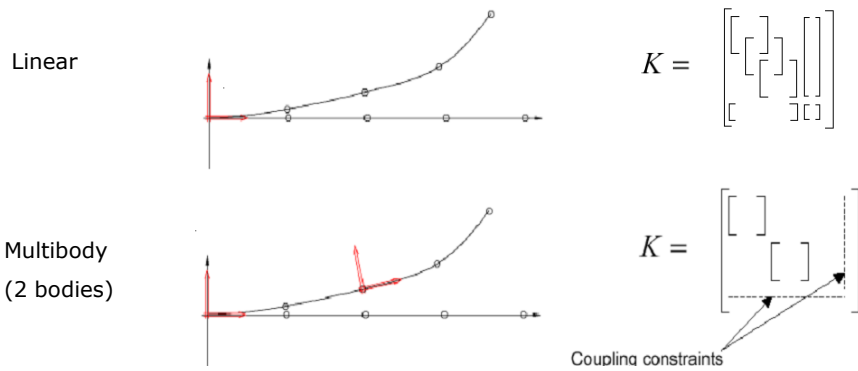
$$\mathbf{r}_p^i = \mathbf{R}^i + \mathbf{A}^i \bar{\mathbf{u}}_p^i$$

$\mathbf{r}_p^i$ : vector in global ref. from origo to point  
 $\mathbf{R}^i$ : vector in global ref. from origo to object origo  
 $\mathbf{A}^i$ : Orientation matrix of local coo related to global coo.  
 $\bar{\mathbf{u}}_p^i$ : vector in local ref. from local origo to point

2 Risø DTU, Technical University of Denmark



## Sub-Structure Kinematics



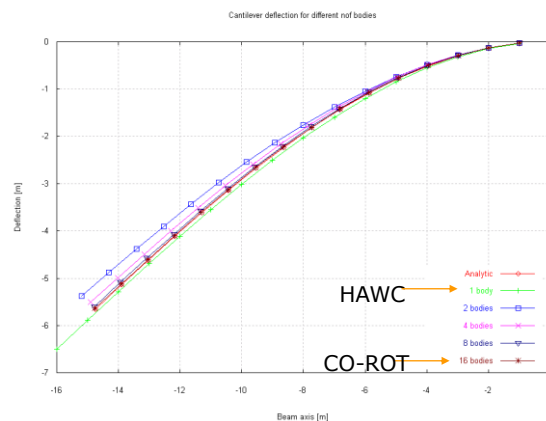
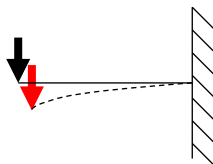
3 Risø DTU, Technical University of Denmark

Structure

## One effect of Multiple Bodies per Blade

Example:

- Bernoulli-Euler cantilever beam loaded by end-load.



4 Risø DTU, Technical University of Denmark

Structure

## Relevance of large rotations ?

Tjæreborg  
10 m/s



External flap/edge loads on blade causes torsion when blades deflect. Main torsion load effect on blades. This also contributes to blade twist.

5 Risø DTU, Technical University of Denmark

Structure

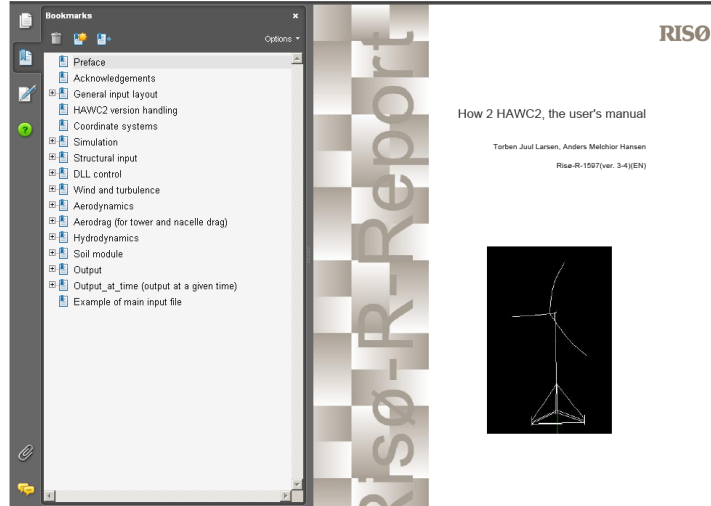
## Main command blocks

```
begin simulation;
-
end simulation;
;
begin main_body;
-
end main_body;
;
begin orientation;
-
end orientation;
;
begin constraint;
-
end constraint;
;
begin wind;
-
end wind;
;
begin aero;
-
end aero;
;
begin dll;
-
end dll;
;
begin output;
-
end output;
```

6 Risø DTU, Technical University of Denmark

Structure

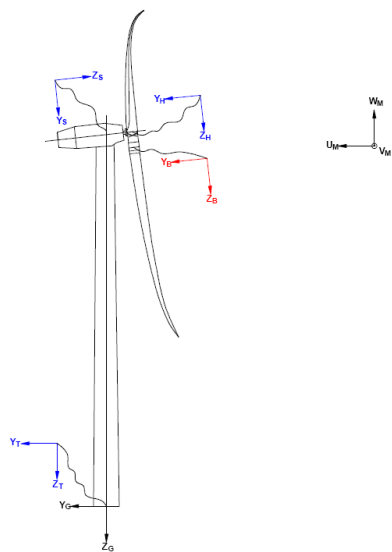
## The manual



## Definitions

- A body is a structural object with its own coo. system and position and orientation according to the global coo. Bodies are connected by constraints.
- To make it convenient for the user the terminology main\_body is often used. This is a body or a structural component which is subdivided into bodies. Could also be understood as a sub structure (Tower, shaft, blade...)
- The main\_body properties must be set up in its own coordinate system first!
- Secondly the initial position, orientation, velocity, rotation velocity must be defined.
- Last the constraints are defined.

# Coordinate systems



9 Risø DTU, Technical University of Denmark

Structure



# Main\_Body example

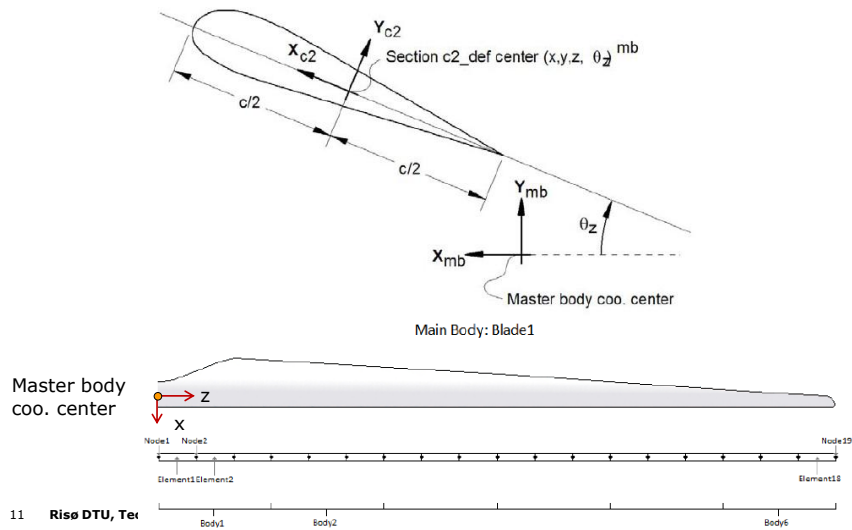
```
begin main_body;
name      bladel ;
type      timoschenko ;
nbodies   6 ;
node_distribution  c2_def;
damping_posdef  1.17e-4 5.77e-5 6.6e-6 6.6e-4 5.2e-4 6.5e-4 ;
begin timoschenko_input ;
filename ./data/st_file.txt ;
set 1 1 ;          set subset
end timoschenko_input;
begin c2_def;      Definition of centerline (main_body coordinates)
nsec 19 ;
sec 1      -0.0000      0.0000      0.000      0.000      ;
sec 2      -0.0041      0.0010      3.278      -13.590      ;
sec 3      -0.1048      0.0250      6.556      -13.568      ;
sec 4      -0.2582      0.0492      9.833      -13.564      ;
sec 5      -0.4694      0.0587      13.111      -13.546      ;
sec 6      -0.5689      0.0957      16.389      -11.406      ;
sec 7      -0.5455      0.0883      19.667      -10.145      ;
sec 8      -0.5246      0.0732      22.944      -9.043      ;
sec 9      -0.4962      0.0669      26.222      -7.843      ;
sec 10     -0.4644      0.0554      29.500      -6.589      ;
sec 11     -0.4358      0.0449      32.778      -5.447      ;
sec 12     -0.4859      0.0347      36.056      -4.234      ;
sec 13     -0.3759      0.0265      39.333      -3.545      ;
sec 14     -0.3453      0.0130      42.611      -2.223      ;
sec 15     -0.3156      0.0084      45.889      -1.553      ;
sec 16     -0.2791      0.0044      49.167      -0.934      ;
sec 17     -0.2675      0.0017      52.444      -0.454      ;
sec 18     -0.1785      0.0003      55.722      -0.121      ;
sec 19     -0.1213      0.0000      59.000      -0.000      ;
end c2_def ;
end main_body;
```

10 Risø DTU, Technical University of Denmark

Structure

## Definition of the centerline

Position and orientation of half chord point related to main body coordinate



11 Risø DTU, Te

## Structural input in data file

```
*****
#1 Main data set number 1 - an example of a shaft structure
*****
More comments space
r      m      x_cg      y_cg      r1_x      r1_y      x_sh      y_sh      E      G      I_x      I_y      K      k_x      k_y      A      theta_s      x_o      y_o
[m]      [kg/m] [m]      [m]      [m]      [m]      [m]      [m]      [N/m^2] [N/m^2] [N/m^4] [N/m^4] [N/m^4] [-]      [-]      [m^2] [deg]      [m]      [m]
#1 10 Sub set number 1 with 10 data rows
0.00 100 0 0 224.18 224.18 0 0 2.10E+11 0.10E+10 1.00E+02 1.00E+02 0.05376 0.52 0.52 0.59 0 0.0 0.0
0.10 100 0 0 224.18 224.18 0 0 2.10E+11 0.10E+10 1.00E+02 1.00E+02 0.05376 0.52 0.52 0.59 0 0.0 0.0
0.1001 1 0 0 0.2 0.2 0 0 2.10E+11 0.10E+10 1.00E+02 1.00E+02 0.05376 0.52 0.52 0.59 0 0.0 0.0
1.00 1 0 0 0.2 0.2 0 0 2.10E+11 0.10E+10 1.00E+02 1.00E+02 0.05376 0.52 0.52 0.59 0 0.0 0.0
1.90 1 0 0 0.2 0.2 0 0 2.10E+11 0.10E+10 1.00E+02 1.00E+02 0.05376 0.52 0.52 0.59 0 0.0 0.0
2.00 1 0 0 0.2 0.2 0 0 2.10E+11 0.10E+10 1.00E+02 1.00E+02 0.05376 0.52 0.52 0.59 0 0.0 0.0
3.00 1 0 0 0.2 0.2 0 0 2.10E+11 0.10E+10 1.00E+02 1.00E+02 0.05376 0.52 0.52 0.59 0 0.0 0.0
3.20 1 0 0 0.2 0.2 0 0 2.10E+11 0.10E+10 1.00E+02 1.00E+02 0.05376 0.52 0.52 0.59 0 0.0 0.0
4.00 1 0 0 0.2 0.2 0 0 2.10E+11 0.10E+10 1.00E+02 1.00E+02 0.05376 0.52 0.52 0.59 0 0.0 0.0
5.0191 1 0 0 0.2 0.2 0 0 2.10E+11 0.10E+10 1.00E+02 1.00E+02 0.05376 0.52 0.52 0.59 0 0.0 0.0
*****
More comments space
r      m      x_cg      y_cg      r1_x      r1_y      x_sh      y_sh      E      G      I_x      I_y      K      k_x      k_y      A      theta_s      x_o      y_o
[m]      [kg/m] [m]      [m]      [m]      [m]      [m]      [m]      [N/m^2] [N/m^2] [N/m^4] [N/m^4] [N/m^4] [-]      [-]      [m^2] [deg]      [m]      [m]
#2 10 As dataset 1, but with 10 data rows
0.00 100 0 0 224.18 224.18 0 0 2.10E+10 0.10E+15 1.00E+02 1.00E+02 0.05376 0.52 0.52 0.59 0 0.0 0.0
0.10 100 0 0 224.18 224.18 0 0 2.10E+10 0.10E+15 1.00E+02 1.00E+02 0.05376 0.52 0.52 0.59 0 0.0 0.0
0.1001 1 0 0 0.2 0.2 0 0 2.10E+10 0.10E+15 1.00E+02 1.00E+02 0.05376 0.52 0.52 0.59 0 0.0 0.0
1.00 1 0 0 0.2 0.2 0 0 2.10E+10 0.10E+15 1.00E+02 1.00E+02 0.05376 0.52 0.52 0.59 0 0.0 0.0
1.90 1 0 0 0.2 0.2 0 0 2.10E+10 0.10E+15 1.00E+02 1.00E+02 0.05376 0.52 0.52 0.59 0 0.0 0.0
2.00 1 0 0 0.2 0.2 0 0 2.10E+10 0.10E+15 1.00E+02 1.00E+02 0.05376 0.52 0.52 0.59 0 0.0 0.0
3.00 1 0 0 0.2 0.2 0 0 2.10E+10 0.10E+15 1.00E+02 1.00E+02 0.05376 0.52 0.52 0.59 0 0.0 0.0
3.20 1 0 0 0.2 0.2 0 0 2.10E+10 0.10E+15 1.00E+02 1.00E+02 0.05376 0.52 0.52 0.59 0 0.0 0.0
4.00 1 0 0 0.2 0.2 0 0 2.10E+10 0.10E+15 1.00E+02 1.00E+02 0.05376 0.52 0.52 0.59 0 0.0 0.0
5.0191 1 0 0 0.2 0.2 0 0 2.10E+10 0.10E+15 1.00E+02 1.00E+02 0.05376 0.52 0.52 0.59 0 0.0 0.0
*****
More comments space
r      m      x_cg      y_cg      r1_x      r1_y      x_sh      y_sh      E      G      I_x      I_y      K      k_x      k_y      A      theta_s      x_o      y_o
[m]      [kg/m] [m]      [m]      [m]      [m]      [m]      [m]      [N/m^2] [N/m^2] [N/m^4] [N/m^4] [N/m^4] [-]      [-]      [m^2] [deg]      [m]      [m]
#3 10 as data set 1 but changed mass properties
0.00 1000 0 0 2.2418 2.2418 0 0 2.10E+11 0.10E+10 1.00E+02 1.00E+02 0.05376 0.52 0.52 0.59 0 0.0 0.0
0.10 1000 0 0 2.2418 2.2418 0 0 2.10E+11 0.10E+10 1.00E+02 1.00E+02 0.05376 0.52 0.52 0.59 0 0.0 0.0
0.1001 1 0 0 0.2 0.2 0 0 2.10E+11 0.10E+10 1.00E+02 1.00E+02 0.05376 0.52 0.52 0.59 0 0.0 0.0
1.00 1 0 0 0.2 0.2 0 0 2.10E+11 0.10E+10 1.00E+02 1.00E+02 0.05376 0.52 0.52 0.59 0 0.0 0.0
1.90 1 0 0 0.2 0.2 0 0 2.10E+11 0.10E+10 1.00E+02 1.00E+02 0.05376 0.52 0.52 0.59 0 0.0 0.0
2.00 1 0 0 0.2 0.2 0 0 2.10E+11 0.10E+10 1.00E+02 1.00E+02 0.05376 0.52 0.52 0.59 0 0.0 0.0
3.00 1 0 0 0.2 0.2 0 0 2.10E+11 0.10E+10 1.00E+02 1.00E+02 0.05376 0.52 0.52 0.59 0 0.0 0.0
3.20 1 0 0 0.2 0.2 0 0 2.10E+11 0.10E+10 1.00E+02 1.00E+02 0.05376 0.52 0.52 0.59 0 0.0 0.0
4.00 1 0 0 0.2 0.2 0 0 2.10E+11 0.10E+10 1.00E+02 1.00E+02 0.05376 0.52 0.52 0.59 0 0.0 0.0
5.0191 1 0 0 0.2 0.2 0 0 2.10E+11 0.10E+10 1.00E+02 1.00E+02 0.05376 0.52 0.52 0.59 0 0.0 0.0
*****
```

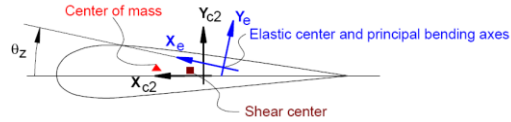
12 Risø DTU, Technical University of Denmark

Structure

## Input columns in data file



Position of structural centers related to c2\_def section coo.



1	r, curved length distance from main_body node
2	m, mass per unit length [kg/m]
3	xm, xc2-coordinate from C1/2 to mass center [m]
4	ym, yc2-coordinate from C1/2 to mass center [m]
5	rix, radius of inertia related to elastic center. Corresponds to rotation about principal bending xe axis [m]
6	riy, radius of inertia related to elastic center. Corresponds to rotation about principal bending ye axis [m]
7	xs, xc2-coordinate from C1/2 to shear center [m]
8	ys, yc2-coordinate from C1/2 to shear center [m]
9	E, modulus of elasticity [N/m2]
10	G, shear modulus of elasticity [N/m2]
11	Ix, area moment of inertia with respect to principal bending xe axis [N/m4]
12	Iy, area moment of inertia with respect to principal bending ye axis [N/m4]
13	K, torsional stiffness constant with respect to ze axis at the shear center [m4/rad]. For a circular section only this is identical to the polar moment of inertia.
14	kx, shear factor for force in principal bending xe direction [-]
15	ky, shear factor for force in principal bending ye direction [-]
16	A, cross sectional area [m2]
17	structural pitch about xc2 axis. This is the angle between the xc2 -axis defined with the c2_def command and the 1st main principal bending axis xe.
18	xe, xc2-coordinate from C1/2 to center of elasticity [m]
19	ye, yc2-coordinate from C1/2 to center of elasticity [m]

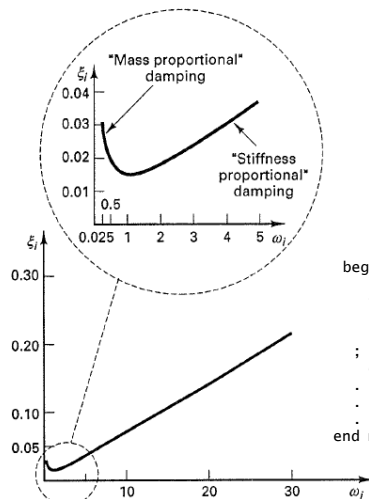
13 Risø DTU, Technical University of Denmark

Structure

## Rayleigh damping parameters



- Mass and stiffness proportional damping parameters need to be given for the vibration direction around the x,y, and z direction.
- Mass proportional damping controls the mean damping level.
- Stiffness proportional damping controls the change with respect to higher frequencies.



```
begin main_body;
  name      blade1 ;
  type      timoschenko ;
  nbodies   9 ;
  node_distribution  c2_def ;
  ; Factors  Mx,  My,  Mz,  Kx,  Ky,  Kz
  damping  3.0e-2  2.2e-2  4.0e-2  5.9e-4  1.9e-3  5.0e-4 ;
  .
  .
end main_body;
```

Figure E9.10 Damping as a function of frequency

14 Risø DTU, Technical University of Denmark

Structure

## Orientation

```
begin orientation;
begin base;
  body tower;
  inipos 0.0 0.0 0.0 ;          initial position of node 1
  body_eulerang 0.0 0.0 0.0;
end base;
;
begin relative;
  body1 tower last;
  body2 shaft 1;
  body2_eulerang 90.0 0.0 0.0;
  body2_eulerang 5.0 0.0 0.0;    5 deg tilt
  body2_ini_rotvec_d1 0.0 0.0 -1.0 0.5 ; body initial rotation velocity x,y,z,angle velocity[rad/s] (body 2 coordinates)
end relative;
;
begin relative;
  body1 shaft last;
  body2 hub1 1;
  body2_eulerang -90.0 0.0 0.0;
  body2_eulerang 2.5 0.0 0.0;    2.5deg cone
end relative;
-
End orientation;
```

## Constraints

- Fix0: This constraint fix node number 1 of a given main\_body to ground.
- Fix1: This constraint fix a given node on one main\_body to another main\_body's node.
- Fix 2: This constraint fix a node 1 on a main\_body to ground in x,y,z direction. The direction that is free or fixed is optional.
- Fix 3: This constraint fix a node to ground in tx,ty,tz rotation direction. The rotation direction that is free or fixed is optional.
- Fix 4: Constraint that locks a node on a body to a another node in translation but not rotation with a prestress feature. The two nodes will start at the defined positions to begin with but narrow the distance until fully attached at time T.



## Constraints

- Bearing 1: Constraint with properties as a bearing without friction. A sensor with same identification name as the constraint is set up for output purpose.
- Bearing 2: This constraint allows a rotation where the angle is directly specified by an external dll action command.
- Bearing 3: This constraint allows a rotation where the angle velocity is kept constant throughout the simulation.
- Bearing 4: This constraint is a cardan shaft constraint. Locked in relative translation. Locked in rotation around one vector and allows rotation about the two other directions.

## Constraints

```
begin constraint;
begin fix0; fixed to ground in translation and rotation of node 1
  body tower;
end fix0;
;
begin bearing1;                                free bearing
  name shaft_rot ;
  body1 tower last;
  body2 shaft 1;
  bearing_vector 2 0.0 0.0 -1.0;                x=coo (0=global,1=body1,2=body2)
end bearing1;
;
begin fix1;
  body1 shaft last;
  body2 hub1 1;
end fix1;
;
begin bearing2;                                forced bearing
  name pitch1;
  body1 hub1 last;
  body2 blade1 1;
  bearing_vector 2 0.0 0.0 -1.0;                x=coo (0=global,1=body1,2=body2)
end bearing2;
;
End constraint;
```

## Natural frequencies

- Commands written in the **new\_htc\_structure** command block

```
; Calculated beam properties of the bodies are written to file
beam_output_file_name ./logfiles/caseid_beam.dat;
; Body initial position and orientation are written to file
body_output_file_name ./logfiles/caseid_body.dat;

; Eigenfrequencies of local body written to file
body_eigenanalysis_file_name ./eigenfrq/caseid_body_eigen.dat;
; Eigenfrequencies and animation files for full turbine modeshapes at
; stand still are written
structure_eigenanalysis_file_name ./eigenfrq/caseid_strc_eigen.dat;
```

## Exercise – structure.htc

- Make a sketch of the modeled turbine including the local main\_body coordinate systems and global coordinates and bearing rotation vectors. Use e.g. the beam\_output\_file\_name and body\_output\_file\_name to help with the overview.
- Calculate natural frequencies of individual bodies and turbine in general. Animate with the animation.exe program.
- Does the frequencies and dampings fit? Tune for better damping.