

HAWC2 course

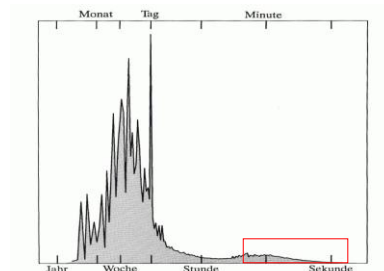
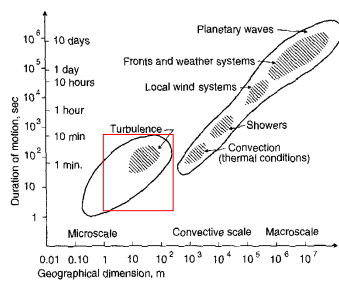
Lesson 2: Wind

$$f(x+\Delta x)=\sum_{i=0}^{\infty}\frac{(\Delta x)^i}{i!}f^{(i)}(x)$$

$$\Delta\int_a^b\Theta^{\sqrt{17}}+\Omega\int\delta e^{i\pi}=\{2.7182818284$$

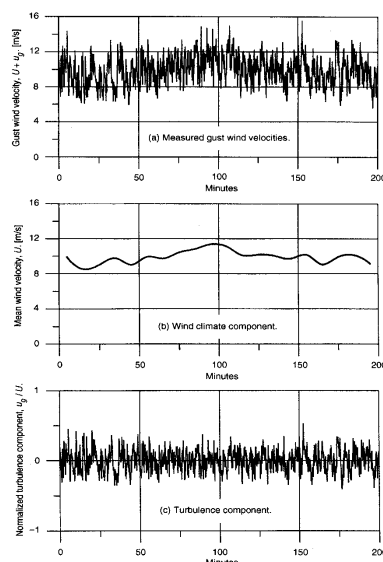
$$\infty=\chi^2\Sigma!>>,\infty$$

Wind systems/ scales



From: M. Courtney, I. Troen: Wind spectrum for one year of continuous 8 Hz measurements. pp 301-304, 9th symposium on Turbulence and diffusion, Denmark 1990.

Mean values and turbulence



Measurement

Variation in wind with frequency content lower than 10min^{-1}

Frequency content higher than 10min^{-1}

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Mean wind and turbulence

Mean wind

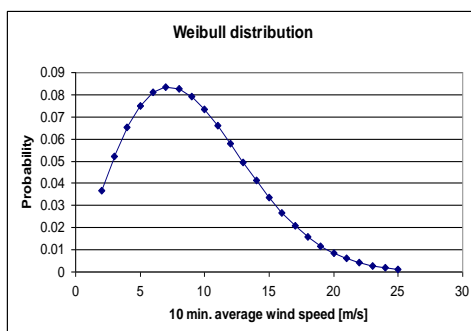
- Hub center wind speed distribution
- Wind shear
- Wind direction
- Slope of mean wind

Turbulence

- Intensity in u-direction
- Relative intensity in v- and w- directions
- Pre-calculated turbulence time series
- [std(U), mean(U), length scale, coherence]

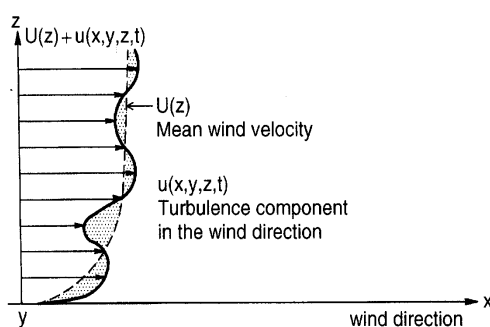
Weibull distribution of mean wind

$$P(U \leq U_0) = 1 - \exp\left(-\frac{U_0^k}{A}\right)$$



$$P(U_0 \leq U \leq U_1) = -\exp\left(-\left(\frac{U_1}{A}\right)^k\right) + \exp\left(-\left(\frac{U_0}{A}\right)^k\right)$$

Wind profile



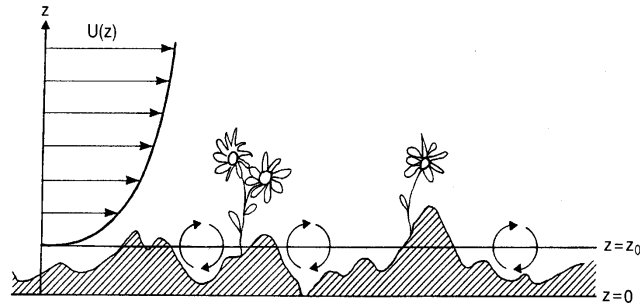
$$U(z) = U_{hub} \frac{\ln(z/z_0)}{\ln(z_{hub}/z_0)}$$

Logarithmic description

$$U(z) = U_{hub} (z/z_{hub})^a$$

Power law description

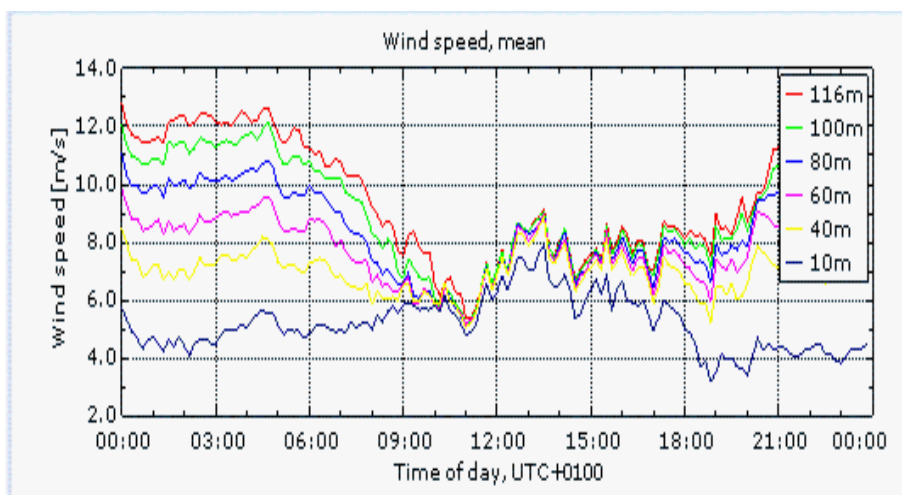
The roughness length, Z_0



- Open sea: 0.0001 m
- Open land: 0.01 m
- Farmland: 0.05 m
- Forrest, city: 0.5-1 m

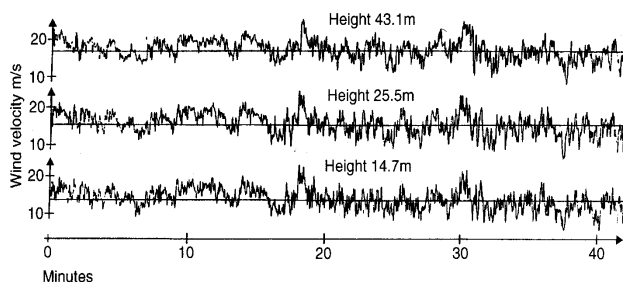
Rotors in atmospheric shear, stability

Met-mast measurements, Høvsøre



from <http://veaonline.risoe.dk>

Turbulence in neutral conditions



For neutral conditions:

$$\sigma = \alpha u_* \quad \text{Monin-Obukhov scaling.}$$

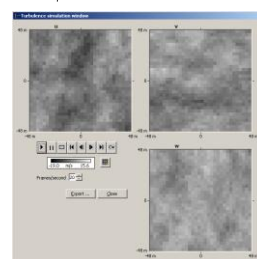
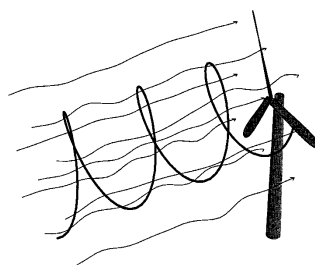
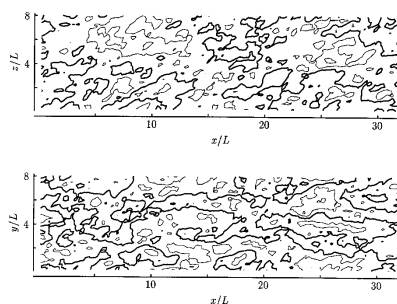
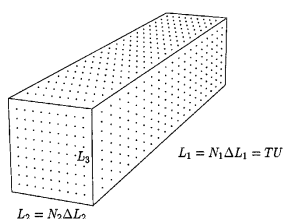
$$\bar{V}(z) = \frac{u_*}{\kappa} \ln(z/z_0), \quad \text{Log. Power law profile}$$

$$I_{amb}(z) = \frac{\alpha \kappa}{\ln(z/z_0)}, \quad \text{where the von Karmans constant } \kappa=0.4 \text{ and } \alpha \sim 2.4$$

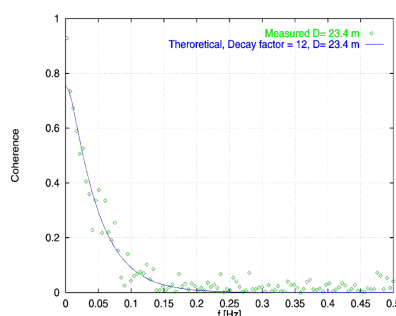
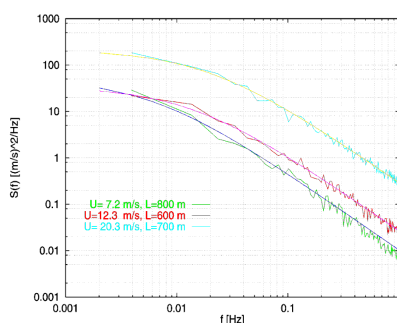
Turbulence intensity is not dependent on wind speed in neutral conditions

$$\sigma(z) = I(z)U(z) = \frac{\alpha \kappa}{\ln\left(\frac{z_{hub}}{z_0}\right)} \quad \text{Standard deviation is constant with height in neutral conditions}$$

Implementation of turbulence in aeroelastic models



Turbulence



$$S_i(f) = \sigma_i^2 \frac{L_i / U}{(1 + 1.5(fL_i / U))^{5/3}}$$

Normal formulation for coherence:

$$coh(r, f) = \exp \left[-A_i \left(\frac{rf}{U} \right) \right]$$

In the IEC standard:

$$coh(r, f) = \exp \left[-12 \sqrt{\left(\frac{rf}{U} \right)^2 + \left(\frac{0.12r}{L_c} \right)^2} \right]$$

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3-D turbulence – typical properties

All components in the turbulence must be included (u,v,w)

$$\frac{s_v}{s_u} = 0.8 \text{ (comp. ter. : : 1.0)}$$

Standard deviation ratio

$$\frac{s_w}{s_u} = 0.5 \text{ (comp. ter. : : 0.8)}$$

$$\frac{L_v}{L_u} = 0.33; \frac{L_w}{L_u} = 0.25$$

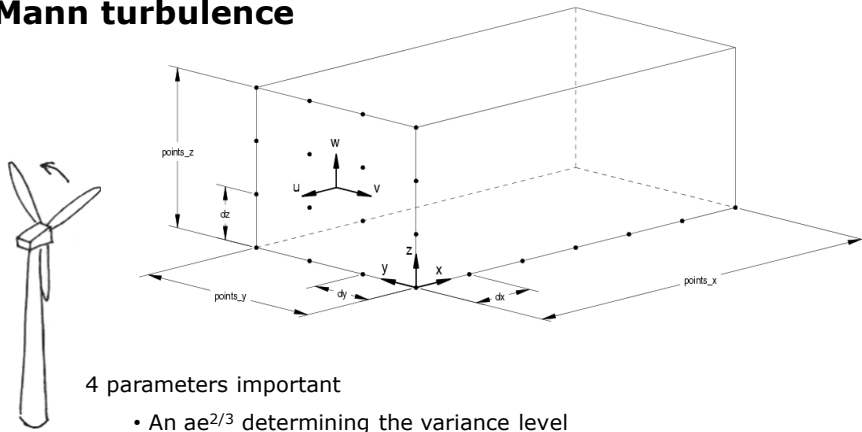
Length scale ratio

When using the Mann model, these properties are given through the gamma parameter (more on this later).

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Mann turbulence



4 parameters important

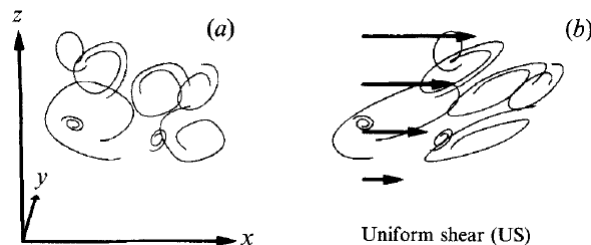
- An $\alpha \varepsilon^{2/3}$ determining the variance level
- A length scale frequency with most energy
- A gamma parameter
- High frequency compensation. (Should the point value represent local vector, or average value for the cell volume)?

Mann turbulence

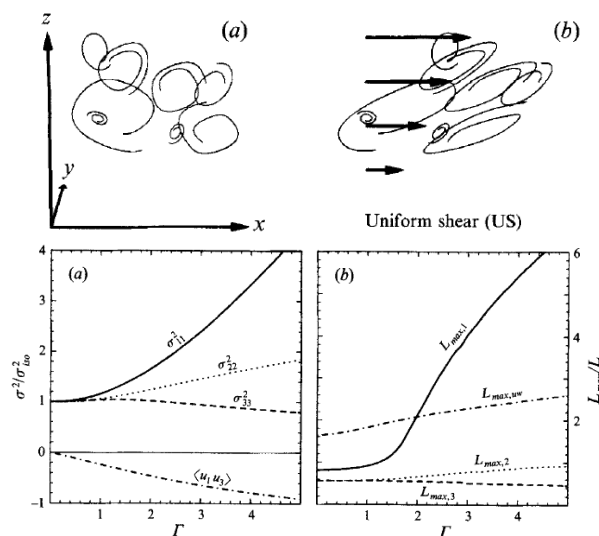
- The turbulence level is in the Mann model obtained through an $\alpha \varepsilon^{2/3}$ parameter in the isotropic energy spectrum (Von Karman).

$$E(k) = \alpha \varepsilon^{\frac{2}{3}} L^{\frac{1}{3}} \frac{(Lk)^4}{(1 + (Lk)^2)^{\frac{17}{6}}},$$

- The spectrum is affected by sheared inflow which modifies the low frequent content and the turbulence level. Γ is a parameter describing the level of shear. $\Gamma=3.9$ correspond to normal conditions.



Turbulence properties as function of Γ



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Turbulence scaling

- Since it is problematic to predict the correct $\alpha \varepsilon^{2/3}$ value to get the requested turbulence level it is much more easy and practically useful to rescale the turbulence field (which is done automatically inside HAWC2).
 - Turbulence field in the center of the box is read and actual variance level found.
 - A scaling factor compensated for difference in variance level is found

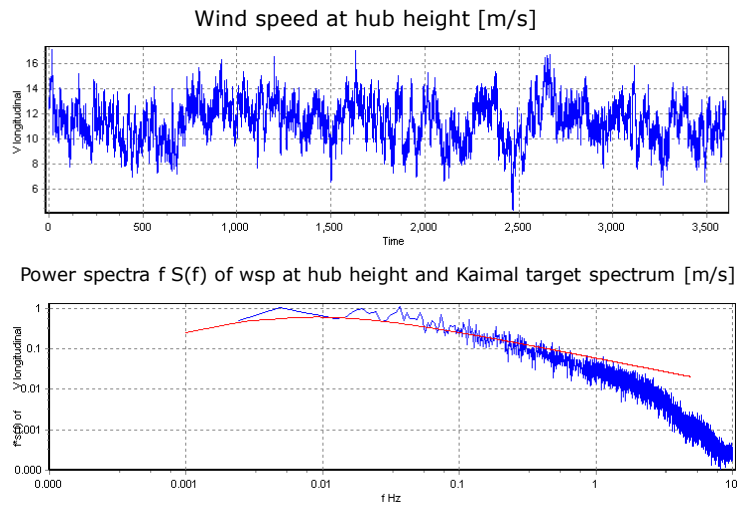
$$SF = \sqrt{\frac{var_{target}}{var}}$$

- This is multiplied to the wind field in u,v and w direction

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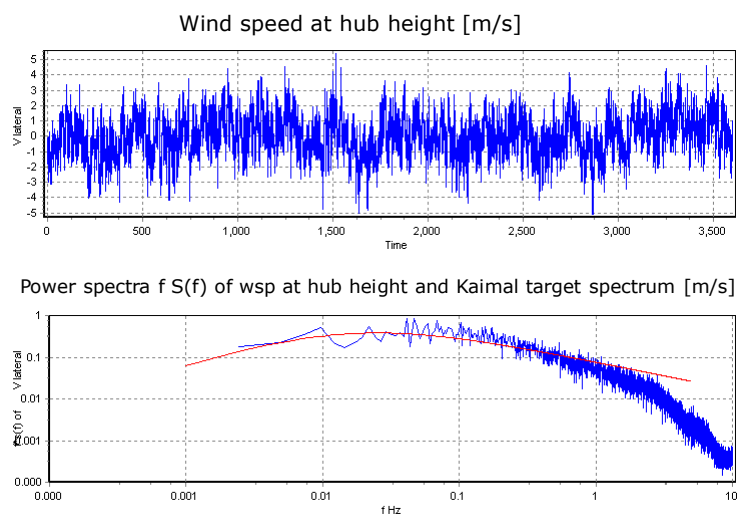
Example at 11.4m/s, u-dir



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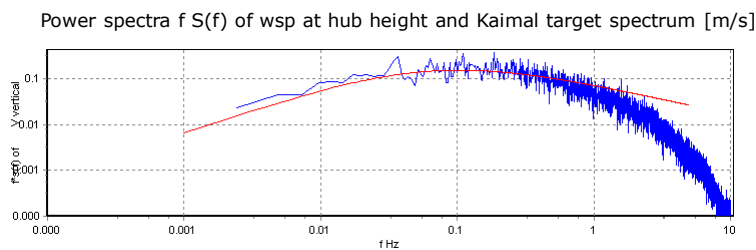
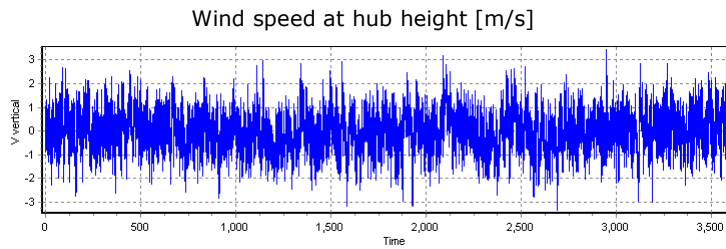
Wind at 11.4m/s, v-dir



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Wind at 11.4m/s, w-dir



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HAWC – wind input



```
begin wind ;
density      1.225 ;
wsp          4 ;
tint         0.15 ;
horizontal_input 1 ;           0=false, 1=true
windfield_rotations 0.0 0.0 0.0 ; yaw, tilt, rotation
center_pos0   0.0 0.0 -123.0 ;
shear_format  3 0.2 ; 0=none, 1=constant, 2=log, 3=power, 4=linear
turb_format   1 ;       0=none, 1=mann, 2=flex
tower_shadow_method 1 ; 0=none, 1=potential flow, 2=jet, 3=pot2, 4=jet2
; scale_time_start 0 ;
; wind_ramp_factor 0.0 40.0 0.5 1.0 ; t0, t1, f0, f1
;
; wind_ramp_abs 50.0 50.1 0.0 1.0 ; t0, t1, v0, v1
; wind_ramp_abs 80.0 80.1 0.0 1.0 ;
;
begin mann;
create_turb_parameters 29.4 1.0 3.9 1025 1.0 ; L, alfaeps, gamma, seed, highfrq compensation
filename_u ./turb/114s1u.bin ;
filename_v ./turb/114s1v.bin ;
filename_w ./turb/114s1w.bin ;
box_dim_u 8192 2.0508 ;
box_dim_v 32 3.125;
box_dim_w 32 3.125;
end mann;
;
begin tower_shadow_potential;
tower_offset 0.0 ;
nsec 2;
radius 0.0 6.0 ;
radius -120.0 2.0 ;
end tower_shadow_potential;
end wind;
;
```

If these files exist, new files will not be created!

The total length of the box should correspond to the simulation length (subtracted the time for initial transients)

$$wsp = \frac{N_x \Delta x}{t_{stop} - t_0}$$

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Generation of very large Turbulence Fields

An example:

Wind speed 11.4m/s

Simulation length 3600s

Fieldsize in meters

41040, 200, 150

No of points in each direction

32768, 64, 32

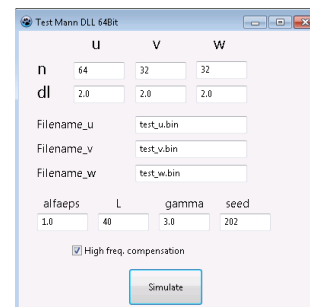
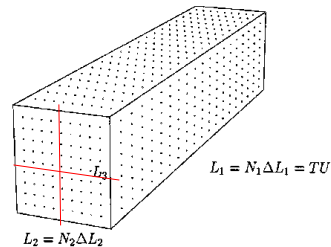
dL1, dL2, dL3

1.252m, 3.125m, 4.68m

dt 0.109s

Memory consumption

3x4x4x32768x64x32=3.2GByte



This cannot be addressed on WIN32. => A new 64 bit application have been made.

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Stability

Until a turbulence model with a buoyancy term is included, the way to model turbulence for different stability class may be through the Mann model using modified parameters

Very Unstable: $L_M = 105.1$
 $\Gamma = 2.1$

Very Stable: $L_M = 10.0$
 $\Gamma = 2.7$

Unstable: $L_M = 80$
 $\Gamma = 2.44$

Stable: $L_M = 15.4$
 $\Gamma = 2.7$

Near Unstable: $L_M = 60.7$
 $\Gamma = 2.8$

Near Stable: $L_M = 28.0$
 $\Gamma = 2.8$

Example:
Unstable
afternoon



Neutral:
 $L_M = 38$
 $\Gamma = 2.7$



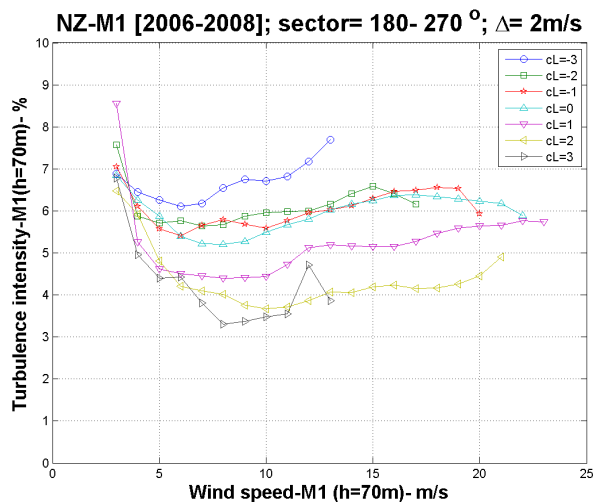
Example
Stable
night

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Stability

Remember the turbulence level is varying with the stability class!



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Tower shadow effects is also part of the wind module

- And so are wake effects from neighboring wind turbines, but this will be presented in a separate lecture

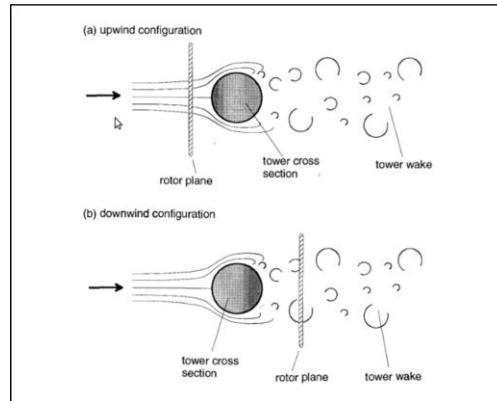
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Tower influence modelling in HAWC2



- models for both an upstream and a downstream position of the rotor is implemented



Tower influence modelling - upstream



Flow model based on the potential flow solution around a cylinder

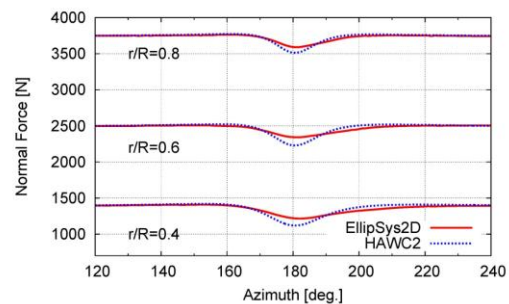
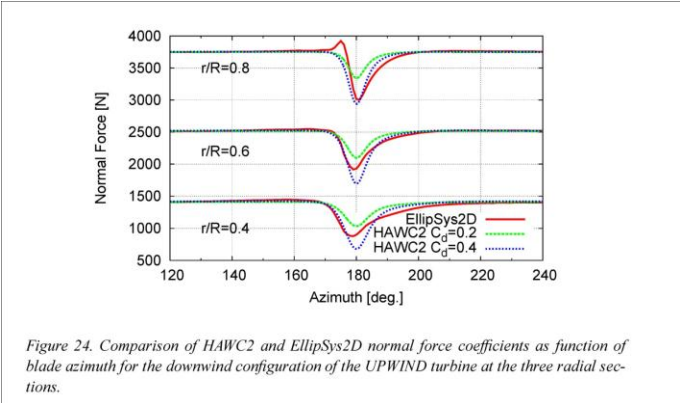


Figure 23. Comparison of HAWC2 and EllipSys2D normal force coefficients as function of blade azimuth for the upwind configuration of the UPWIND turbine at the three radial sections.

Tower influence modelling - downstream

DTU

Flow model based on the boundary solution for a jet into a flow at rest



Tower influence modelling - downstream

DTU

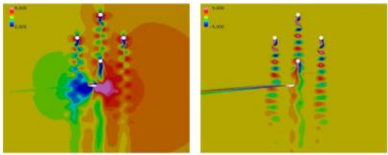
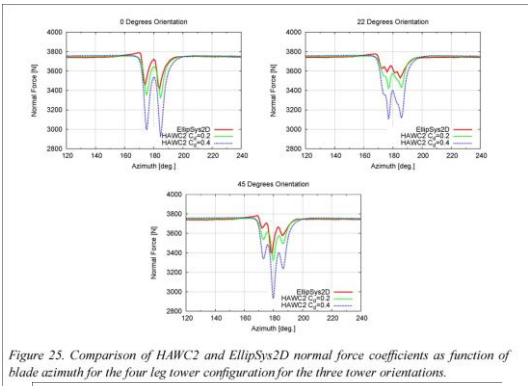


Figure 22. Snapshot of axial velocity and vorticity for the four leg configuration for the 80% radius blade section at 45 degrees orientation to the tower.

HAWC – wind input

```
begin wind ;
density      1.225 ;
wsp          4 ;
tint         0.15 ;
horizontal_input 1 ;           0=false, 1=true
windfield_rotations 0.0 0.0 0.0 ; yaw, tilt, rotation
center_pos0  0.0 0.0 -123.0 ;
shear_format 3 0.2 ; 0=none, 1=constant, 2=log, 3=power, 4=linear
turb_format  1 ; 0=none, 1=mann, 2=flex
tower_shadow_method 1 ; 0=none, 1=potential flow, 2=jet, 3=pot2, 4=jet2
;
begin tower_shadow_potential;
tower_offset 0.0 ;
nsec 2;
radius 0.0 6.0 ; z, radius
radius -120.0 2.0 ;
end tower_shadow_potential;
;
begin tower_shadow_jet;
tower_offset 0.0 ;
nsec 2;
radius 0.0 6.0 1.0 ; z, radius, cd
radius -120.0 2.0 1.0;
end tower_shadow_jet;
end wind;
;
```